

Rough Subspace Error Correcting Output Codes

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1. Multiclass Classification

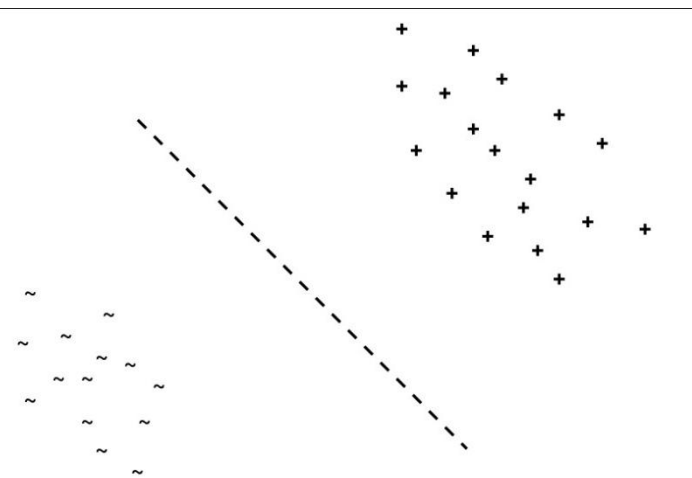
2. Rough Subspace ECOC

3. Experiments

4. Conclusions

Introduction: Multiclass Classification

- Class binarization
- Decomposition frameworks
 - One-versus-all (OvA)
 - One-versus-one (OvO)
 - Error Correcting Output Codes (ECOC)

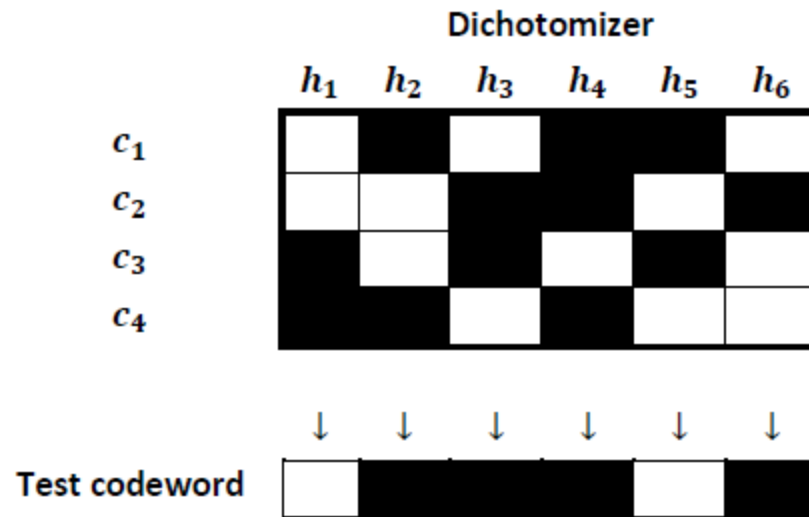


(b) One-versus-One Classification
 $c(c-1)/2$ classifiers, one for each pair of classes.
Here: + against ~

Error Correcting Output Codes

- Introduction
- Coding
 - Binary vs. Ternary
 - Static vs. Dynamic

- Decoding



Analysis of ECOC

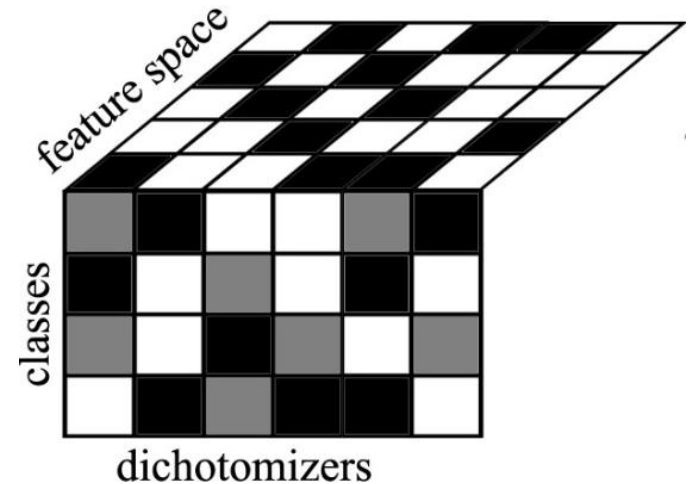
- Introduction
 - The focus of the ECOC-based methods:
maximizing row and/or column separation
- **Independence**
cornerstone of the ECOC framework
- **Accuracy**

Analysis of ECOC (*cont.*)

- Discussion on the strategies in the ECOC literature for designing independent classifiers
- Analysis of results of
 - (García-Pedrajas and Ortiz-Boyer, 2011)
 - (Dietterich and Bakiri, 1995, Shapire, 1997)
- Therefore, ...

2. Subspace Approach to Error Correcting Output Codes

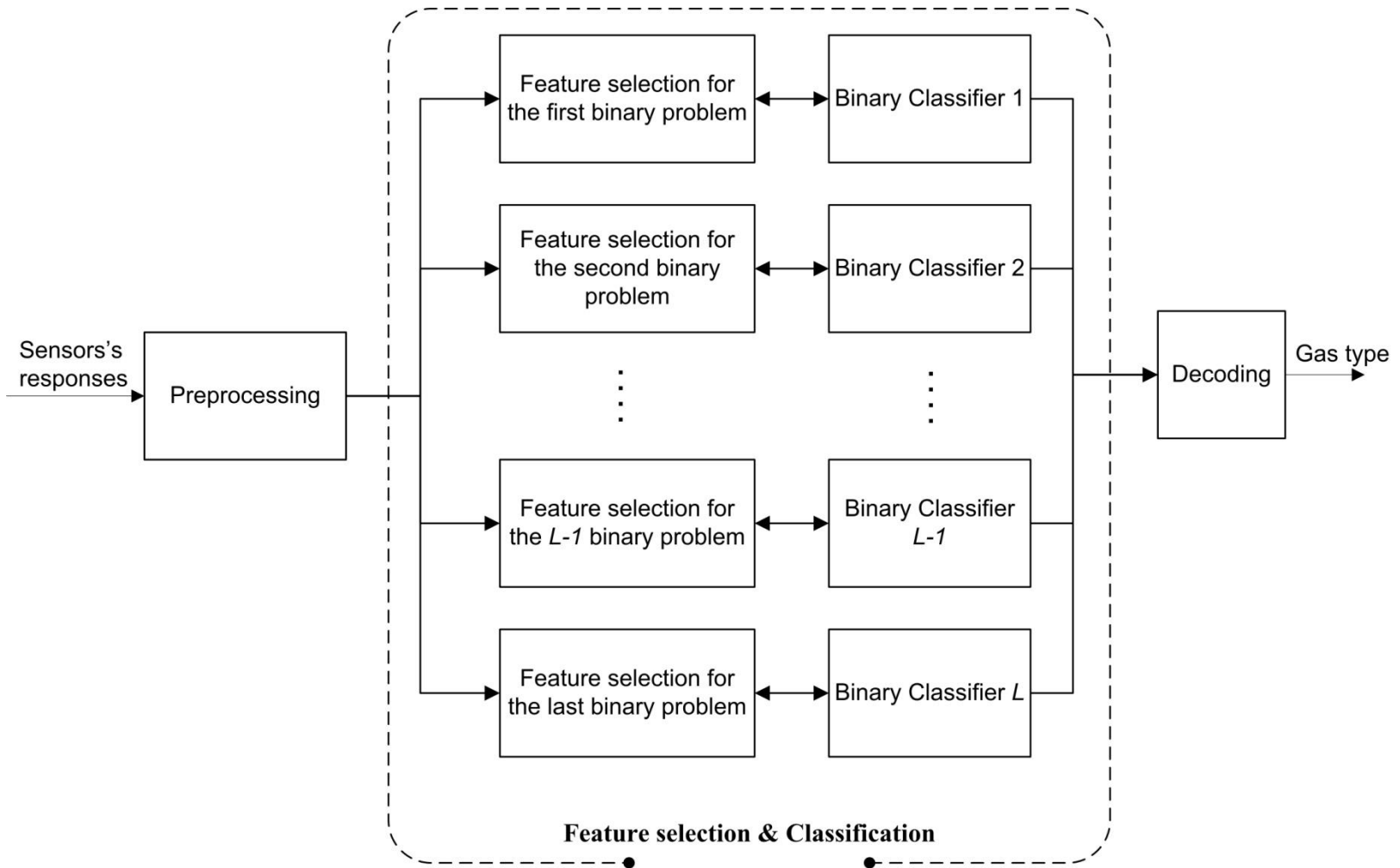
- Idea of subspace approach
- Core of the proposed method: Subspace ECOC



- Advantages
 - More independent classifiers
 - More accurate classifiers (provided that ...)
 - Longer ECOC codes

Rough set subspace ECOC

- Challenges
 - 1) How to find good feature subsets?
 - 2) How many feature subsets should be selected for each dichotomizer?
- Out solutions (out of many!)
 - 1) Rough Set Feature Selection
 - 2) 10 feature subsets (reduct sets)



QuickMultipleReduct algorithm

QuickMultipleReduct (C, D, N)

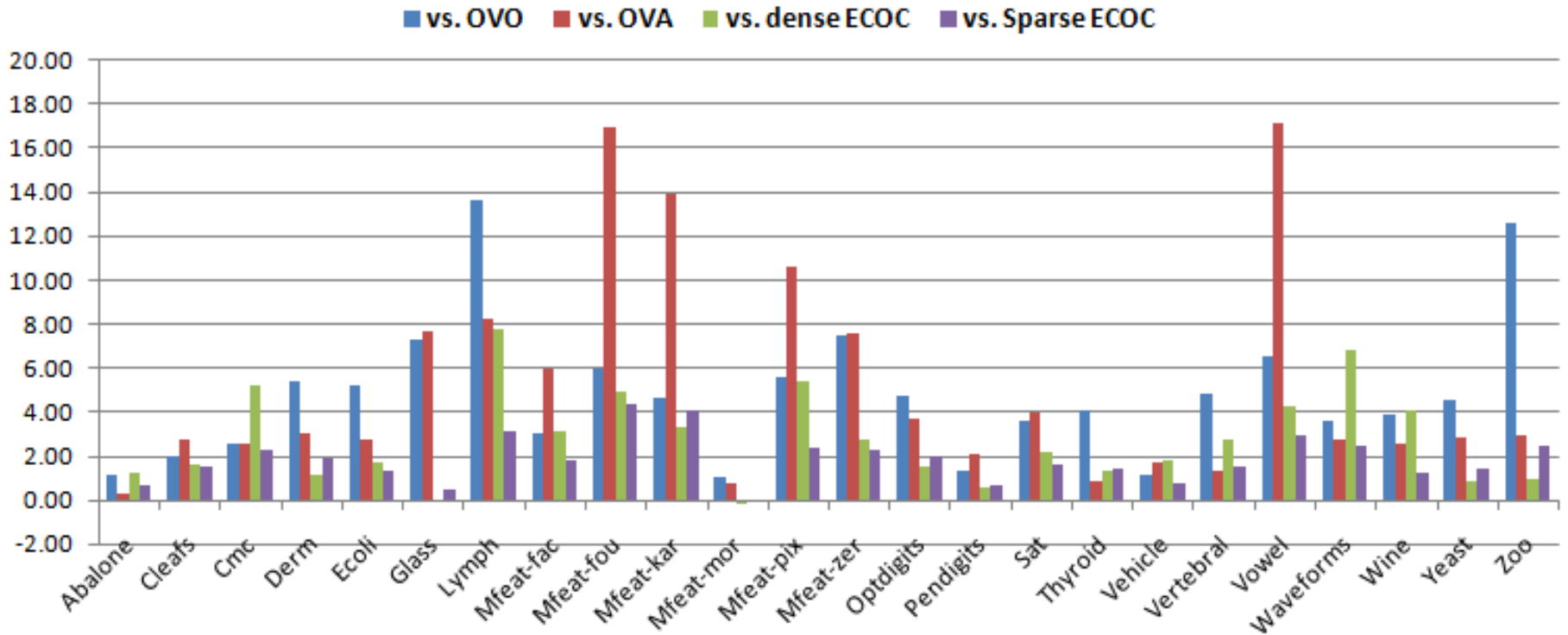
- C : the set of all conditional features.
- D : the set of decision features.
- N : number of reduct sets per dichotomizer.

1. $\forall f \in C,$
2. $\Gamma(\cdot) = \gamma_f(D)$
3. Sort Γ on descending order
4. For $i = 1:N$
5. $\text{rand} = \text{unirand}(|C|/2)$ // generate a uniform random number
6. $\text{Init}_f = \Gamma(\text{rand})$
7. $R_i \leftarrow \{\text{Init}_f\}$
8. do
9. $T \leftarrow R_i$
10. $\forall f \in (C - R_i)$
11. if $\gamma_{R_i \cup \{f\}}(D) > \gamma_T(D)$
12. $T \leftarrow R_i \cup f$
13. $R_i \leftarrow T$
14. until $\gamma_{R_i}(D) = \gamma_C(D)$
15. $\text{MultipleReducts}\{i\} = R_i$
16. end
17. Return *MultipleReducts*

Experimental evaluation over benchmark datasets

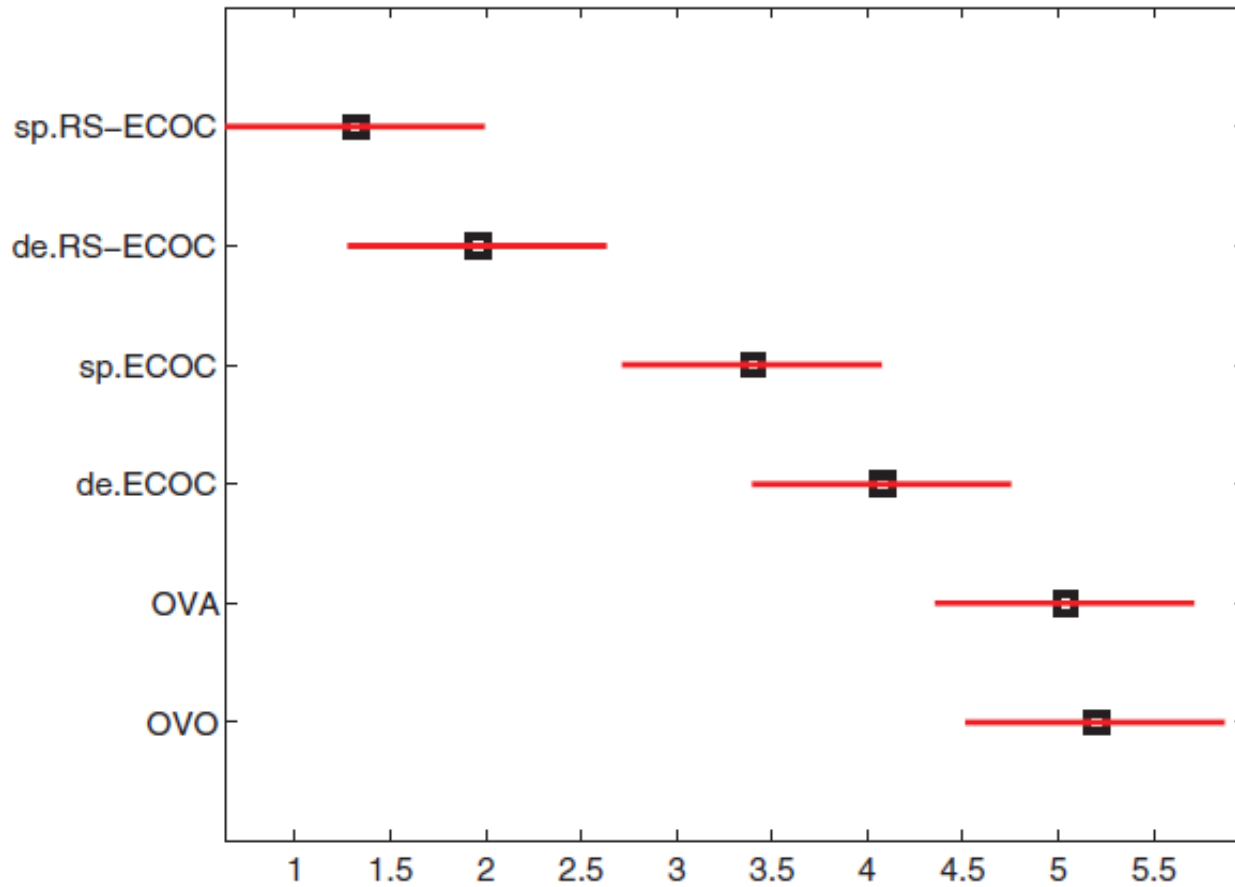
	Dataset	# instances	# features	# classes
1	Abalone	4177	8	3
2	Cleafs	4758	64	8
3	Cmc	1473	9	3
4	Derm	358	34	6
5	Ecoli	336	7	8
6	Glass	214	9	6
7	Lymph	148	18	4
8	Mfeat-fac	2000	216	10
9	Mfeat-fou	2000	76	10
10	Mfeat-kar	2000	64	10
11	Mfeat-mor	2000	6	10
12	Mfeat-pix	2000	240	10
13	Mfeat-zer	2000	47	10
14	Optdigits	5620	64	10
15	Pendigits	10992	16	10
16	Sat	6435	36	6
17	Thyroid	215	5	3
18	Vehicle	846	18	3
19	Vertebral	310	6	3
20	Vowel	528	10	11
21	Waveforms	5000	40	3
22	Wine	178	13	3
23	Yeast	1484	8	10
24	Zoo	101	16	7

Experimental results



Advanced classification accuracy of the RSS-ECOC in comparison with rival methods

Statistical analysis



(b) MLP Classifier

Conclusions

- Summary of the ECOC analysis
- Research contribution
- When the subspace approach works?
- Computational complexity

Thanks

